



Holy Trinity and S.Silas

Calculation Policy

**Progression grids for written methods for
addition, subtraction, multiplication and division**

Simple progression in written methods for addition

Children need to be able to:

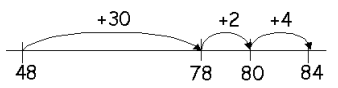
- recall addition pairs to $9 + 9$
- know all complements to 10
- add mentally a series of single-digit numbers, such as $5 + 8 + 4$
- count on in 1s, 10s and 100s
- partition numbers in ways other than into tens and ones to help with bridging multiples of 10 and 100

Stage 1: Empty number line

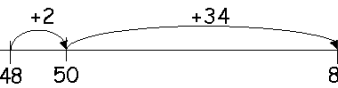
The empty number line helps to record the steps on the way to calculating the total. The steps often bridge through a multiple of 10.

Example:

$48 + 36 = 84$



or:



Children need to be able to:

- partition numbers into hundreds, tens and ones
- recall addition pairs to $9 + 9$
- add multiples of 10 or 100 (such as $60 + 70$ or $600 + 700$) using a related fact ($6 + 7$) and knowledge of place value
- mentally add multiples of 100, 10 and 1 e.g. $800 + 130 + 12$

Stage 2: Partitioning

When adding larger numbers, it becomes less efficient to count on so partitioning is used. Partition into (hundreds) tens and ones, add to form partial sums and then recombine.

Partitioning all the numbers mirrors the standard column method where ones are placed under ones and tens under tens etc.

Example:

Partitioned numbers are written under one another:

$$47 + 76 = 40 + 7$$

$$= \underline{70} + \underline{6}$$

$$110 + 13 = 123$$

$$375 + 567 = 300 + 70 + 5$$

$$\underline{500} + \underline{60} + \underline{7}$$

$$800 + 130 + 12 = 942$$

Stage 3: Expanded column method

The expanded method leads children to the more compact column method so that they understand the structure and efficiency of it.

The amount of time that should be spent teaching and practising the expanded method will depend on how secure the children are in their recall of number facts and in their understanding of place value.

Example:

Write the numbers in columns:

Add the ones first
$\begin{array}{r} 47 \\ + 76 \\ \hline 13 \\ \hline 110 \\ 123 \end{array}$

Discuss how adding the ones first gives the same answer as adding the tens first. Refine over time to consistently adding the ones digits first. The addition of the tens in the calculation $47 + 76$ is described as 'Forty plus seventy equals one hundred and ten', stressing the link to the related fact 'Four plus seven equals eleven'.

Stage 4: Column method

The method is then shortened and when the column total is a two-digit number, the tens (or hundreds) are carried over into the next column. Use the words 'carry ten' or 'carry one hundred', **not** 'carry one'.

Example:

$\begin{array}{r} 366 \\ + 458 \\ \hline 824 \\ \hline 11 \end{array}$
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Once learned, this method is quick and reliable. Later, extend to adding three two-digit numbers, two three-digit numbers, and numbers with different numbers of digits. This method of can also be used to add decimals.

Simple progression in written methods for subtraction

Children need to be able to:

- recall all addition and subtraction facts to 20;
- subtract multiples of 10 (such as $160 - 70$) using the related subtraction fact ($16 - 7$) and their knowledge of place value
- know all complements to 10 and 100

Children need to be able to:

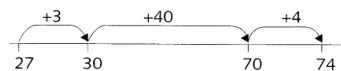
- partition two-digit and three-digit numbers into multiples of one hundred, ten and one
- partition numbers in different ways. e.g. 74 into $70 + 4$ or $60 + 14$
- subtract mentally a single-digit number or a multiple of 10 from a two-digit number
- add the totals (of the hundreds, tens and ones columns) mentally

Stage 1: Empty number line

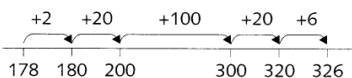
Empty or numbered lines are a useful way of modelling processes such as bridging through multiples of ten. The steps can be recorded by counting on or back.

Find the difference by counting on:

$$74 - 27 = 47$$



$$326 - 178 = 148$$



Counting back example:

$$15 - 7 = 8$$



$$74 - 27 = 47$$



The steps may be recorded in a different order or combined. With practice children will record less information and decide whether to count on or back

Stage 2: Column counting on method for Subtraction

Example

Set calculation out as below. Use the lower integer as your starting point and the larger integer as your 'target number.' Round lower to the next multiple of 10. The jump to the multiple of 10 before your target number, before finally arriving at your target number, e.g.

$$\begin{array}{r} 74 \\ 27 - \\ \hline 3 \text{ (to make 30)} \\ 40 \text{ (to make 70)} \\ 4 \text{ (to make 74)} \\ - \\ 47 \end{array}$$

Add all numbers together to find the difference.

Example

Set calculation out as below. Use the lower integer as your starting point and the larger integer as your 'target number.' Round lower to the next multiple of 10. Then jump to the next multiple 100, then the multiple of 100 before your target number, before doing one final big jump to your target number, e.g.

$$\begin{array}{r} 563 \\ 271 - \\ \hline 9 \text{ (to make 280)} \\ 20 \text{ (to make 300)} \\ 200 \text{ (to make 500)} \\ 63 \text{ (to make 563)} \\ - \\ 292 \end{array}$$

Add all numbers together to find the difference.

Stage 3: Decomposition

$$\begin{array}{r} 674 \\ -27 \\ \hline 47 \end{array}$$

Say, "60 - 20" or, "6 tens - 2 tens" not, "6 - 4"

$$\begin{array}{r} 4563 \\ -271 \\ \hline 292 \end{array}$$

Say, "60 - 20" or, "6 tens - 2 tens" not, "6 - 4"

Simple progression in written methods for multiplication

Children need to be able to:

- count in steps
- understand multiplication as repeated addition

Children need to be able to:

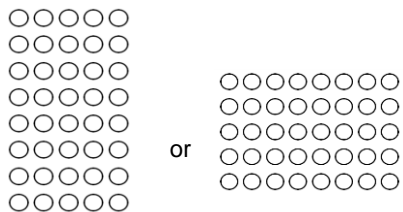
- partition numbers into multiples of one hundred, ten and one and in other ways
- recall multiplication facts to 10×10
- work out products such as 70×5 , 70×50 , 700×5 , or 700×50 , using the related fact, 7×5 , and an understanding of place value
- add combinations of numbers mentally or using a written method

Stage 1: Repeated addition

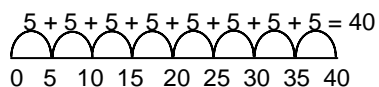
Children start by understanding multiplication as arrays and repeated addition. They use this understanding to help them work out multiplication facts they cannot recall quickly

Example:

For '8 x 5', children picture:



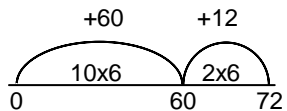
They use repeated addition to work out the calculation:



Recording of the steps on the number line may be refined as understanding and knowledge of facts develops:

Example:

12×6



This will support children in learning their tables using known facts and in understanding the distributive law which they will apply later when using the grid method.

Stage 2: Grid method

When multiplying a 1-digit number by a 2-digit number, children may choose to partition the numbers in different ways:

Example: For 7×38

x	30	8
7		

Larger number along the top

Ensure that children understand the relationship between 7×3 and 7×30 and are not simply 'adding a nought'

The same method can also be applied when multiplying a 1-digit number by a 3-digit number:

X	500	40	9
6	3000	240	54
			3294

Ensure that children understand the relationship between 6×5 and 6×500 and are not simply 'adding 2 noughts'

Example: When multiplying a 2-digit number by a 2-digit number:

(1) Partition both numbers and multiply each part

(2) Add the answers in each row

(3) Add the two row totals to find the final product

	X	20	7		X	20	7	Tot		X	20	7	
	50	1000	350		50	1000	350	1350		50	1000	350	1350
	6	120	42		6	120	42	162		6	120	42	162
													1512

Stage 3: Short/long multiplication

Example:

$$\begin{array}{r} 38 \\ \times 7 \\ \hline 56 \\ 210 \\ \hline 266 \end{array}$$

Children describe what they are doing by referring to the value of the digits. Say, "30x7", not "3x7" although the relationship should be stressed

$$\begin{array}{r} 549 \\ \times 6 \\ \hline 54 \\ 240 \\ 3000 \\ \hline 3294 \end{array}$$

Children say, "6x9, 6x40, 6x500"

$$\begin{array}{r} 56 \\ \times 27 \\ \hline 42 \\ 350 \\ 120 \\ \hline 1000 \\ \hline 1512 \end{array}$$

Children say, "7x6, 7x50, 20x6, 20x50"

Simple progression in written methods for division

Children need to be able to:

- understand division as grouping and sharing
- understand multiplication and division as inverse operations
- recall multiplication and division facts to 10×10
- understand remainders
- derive larger multiples using known facts e.g. $10 \times 3 = 30 \rightarrow 20 \times 3 = 60$
- add multiples mentally and work out differences

Children need to be able to:

- Use known facts
- Use multiples of 1, 2, 5, 10 and 20 to derive facts

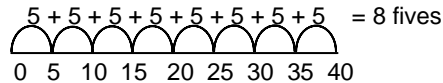
Use with the most able children who have a secure understanding of all the previous steps.

Stage 1: Repeated addition

When it is not appropriate to use a sharing method for division and the division fact is not known, repeated addition (using the relationship between multiplication and division) can be used.

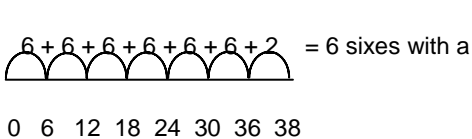
Example without remainder:

$40 \div 5$
Ask "How many 5s in 40?"



Example with remainder:

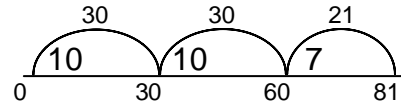
$38 \div 6$
remainder of 2



For larger numbers, when it becomes inefficient to count in single multiples, bigger jumps can be recorded using known facts.

Example without remainder:

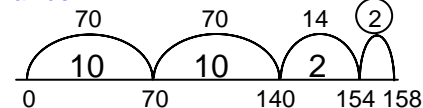
$81 \div 3$



This could either be done by working out the numbers of threes in each jump as you go along (10 threes are 30, another 10 threes makes 40, and another 7 threes makes 81. That's 27 threes altogether) or by counting in jumps of known multiples of 3 to reach 81 ($30 + 30 + 21$) then working out the number of threes in each jump.

Example with remainder:

$158 \div 7$



10 sevens are 70, add another 10 sevens is 140, add 2 more sevens is 154 add 2 makes 158. So there are 22 sevens with a remainder of 2.

The remainder is indicated above the jump rather than inside it, so that children do not mistakenly add 10, 10, 2 and 2 and get an answer of 24.

Stage 2: Chunking on a numberline

Example

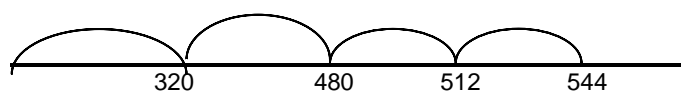
544 divided by 16

Build up and derive facts, i.e. use what the children already know to start:

$1 \times 16 = 16$
 $2 \times 16 = 32$
 $5 \times 16 = 80$
 $10 \times 16 = 160$
 $20 \times 16 = 320$

It is useful for children to derive $1x$ and $10x$ a number and then work out $2x$, $5x$ and $20x$ – as they can use halving and doubling

20×16 10×16 2×16 2×16

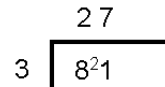


Repeated subtraction (Chunking method)

Stage 3: Short division

Example without remainder:

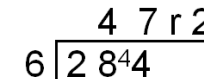
$81 \div 3$



Children use their knowledge of the 3 times table to find, "How many 3s in 80 where the answer is a multiple of 10?" This gives 20 threes (since 30 threes would be too many), with 20 remaining (2 tens are carried over to the next column) Now ask: "How many threes in 21".

Example with remainder:

$284 \div 6$



Once children's understanding of this method is secure they might shorten their dialogue to:

"How many 6s in 28?"
"4 remainder 4"
"How many 6s in 44?"
"7 remainder 2"

BUT ensure children have a secure understanding of what they are doing and are able to use their knowledge of related facts to either make a rough estimate first or have an idea about whether their final answer is reasonable or not.
Division with decimals
Division with the traditional long method